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# A first-principles comparison of the electronic properties of $\text{MgC}_y\text{Ni}_3$ and $\text{ZnC}_y\text{Ni}_3$ alloys

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## Abstract

First-principles, density-functional-based electronic structure calculations are employed to study the changes in the electronic properties of  $\text{ZnC}_y\text{Ni}_3$  and  $\text{MgC}_y\text{Ni}_3$  using the Korringa–Kohn–Rostoker coherent-potential approximation method in the atomic sphere approximation (KKR-ASA CPA). As a function of decreasing C atomic percentage, we find a steady decrease in the lattice constant and bulk modulus in both alloys. However, the pressure derivative of the bulk modulus displays an opposite trend. Following the Debye model, which relates the pressure derivative of the bulk modulus to the average phonon frequency of the crystal, it can thus be argued that  $\text{ZnCNi}_3$  and its disordered alloys possess a different phonon spectrum in comparison to its  $\text{MgCNi}_3$  counterparts. This is further justified by the marked similarity we find in the electronic structure properties such as the variation in the density of states and the Hopfield parameters calculated for these alloys. The effects on the equation of state parameters and the density of states at the Fermi energy, for partial replacement of Mg by Zn, are also discussed.

## 1. Introduction

In spite of being iso-structural and iso-valent to the cubic perovskite 8 K superconductor  $\text{MgCNi}_3$  [1],  $\text{ZnCNi}_3$  remains in the normal metal state down to 2 K [2]. Specific heat measurements indicate that the absence of superconductivity in  $\text{ZnCNi}_3$  may be due to a substantial decrease in the density of states at the Fermi energy  $N(E_F)$  resulting from its relatively low unit cell volume in comparison with  $\text{MgCNi}_3$  [2]. However, electronic structure calculations show that the decrease in  $N(E_F)$  is not sizeable enough to make  $\text{ZnCNi}_3$  non-superconducting [3]. For both  $\text{MgCNi}_3$  [4–7] and  $\text{ZnCNi}_3$  [3], the density of states spectra display similar characteristics, particularly in the distribution of electronic states near the Fermi energy  $E_F$ . The electronic states at  $E_F$  are dominated by Ni 3d states with a little admixture of C 2p states. There exists a strong van Hove singularity-like feature just below  $E_F$ , which is primarily derived from the Ni 3d bands.

To account for the lack of superconductivity in  $\text{ZnCNi}_3$ , the density-functional-based calculations emphasize that the material subjected to the specific heat measurements may be non-stoichiometric in the C sub-lattice [3]. This would then make it similar to the  $\alpha$ -phase of  $\text{MgCNi}_3$ , which has a low unit cell volume and remains non-superconducting [8]. It has been shown earlier that the exact C content in  $\text{MgC}_y\text{Ni}_3$  depends on the nature of synthesis and other experimental conditions [1, 8–12]. According to Johannes and Pickett [3], the arguments that favour non-stoichiometry are the following. (i) Total energy minimization en route to equilibrium lattice constant within the local-density approximation (LDA) finds an overestimated value for  $\text{ZnCNi}_3$  in comparison with the experimental values. In general, overestimation is not so common in the LDA. Meanwhile, when one uses a similar technique for  $\text{MgCNi}_3$ , the calculations find a slightly underestimated value which is consistent within the limitations of the density-functional theory [4, 13, 14]. (ii) The authors also find  $N(E_F)$  in  $\text{MgCNi}_3$  estimated as 13.6 states/Ryd atom, while for  $\text{ZnCNi}_3$ , under similar approximations, it was found to be 11.01 states/Ryd atom. Note that it has been shown both experimentally as well as from first-principles calculations that a decrease in the lattice constant or a decrease in the C occupancy would lead to a decrease in  $N(E_F)$  [13]. (iii) A decrease in the unit cell dimensions can induce phonon hardening. This is well supported by experiments which find the Debye temperature to be approximately 1.6 times higher for  $\text{ZnCNi}_3$  in comparison to  $\text{MgCNi}_3$  [2].

Earlier synthesis of  $\text{ZnC}_y\text{Ni}_3$  [15–17] found the lattice constant to be 6.899 au, for which the occupancy in the C sub-lattice was just 70%. The authors have employed a similar preparation technique for  $\text{MgCNi}_3$  [15] and have found that the C occupancy ranges between 0.5–1.25, which is consistent with the recent reports [1, 8–12, 18]. A lattice constant for  $\text{ZnCNi}_3$  as high as 7.126 au has also been reported elsewhere [19, 20], which then becomes consistent with the recent total energy minimized value using density-functional-based methods. Hence, it seems that  $\text{ZnCNi}_3$  which was subjected to specific heat experiments [2] may indeed suffer from non-stoichiometry.

To understand and compare the effects of C stoichiometry on the structural and electronic properties of  $\text{MgC}_y\text{Ni}_3$  and  $\text{ZnC}_y\text{Ni}_3$ , we carried out a detailed study using the Korringa–Kohn–Rostoker (KKR) Green’s function method [21, 22] formulated in the atomic sphere approximation (ASA) [23]. For disorder, we employ the coherent-potential approximation (CPA) [24]. Characterization of  $\text{MgC}_y\text{Ni}_3$  and  $\text{ZnC}_y\text{Ni}_3$  with  $0.85 \leq y \leq 1.00$  mainly involves the changes in the equation of state parameters, namely, the equilibrium lattice constant, bulk modulus and its pressure derivative. The electronic structure is studied with the help of the total and the sub-lattice resolved densities of states. The propensity of magnetism in these materials is studied with the help of fixed-spin moment method [25] in conjunction with the Landau theory of phase transition [26]. The Hopfield parameter  $\eta$  which generally maps the local ‘chemical’ property of an atom in a crystal is also calculated as suggested by Skriver and Mertig [27], and its variation as a function of lattice constant has also been studied. In general, we find that both  $\text{MgCNi}_3$  and  $\text{ZnCNi}_3$  display very similar electronic structure. Evidence suggests that the non-superconducting nature of  $\text{ZnCNi}_3$  may be related to the crystal structure characteristics, namely the phonon spectra.

## 2. Computational details

The ground state properties of  $\text{MgC}_y\text{Ni}_3$  and  $\text{ZnC}_y\text{Ni}_3$  were calculated using the KKR-ASA-CPA method of alloy theory. For improving alloy energetics, the ASA was corrected by the use of both the muffin-tin correction for the Madelung energy [28] and the multi-pole moment correction to the Madelung potential and energy [29, 30]. These corrections have

brought significant improvement in the accuracy of the total energy by taking into account the non-spherical part of polarization effects [31]. The partial waves in the KKR-ASA calculations are expanded up to  $l_{\max} = 3$  inside atomic spheres, although the multi-pole moments of the electron density have been determined up to  $l_{\max}^M = 6$ , which is used for the multi-pole moment correction to the Madelung energy. In general, the exchange–correlation effects are taken into consideration via the local-density approximation with Perdew and Wang parameterization [32], although a comparison in the equation of state parameters has been made in this work with the generalized gradient approximation (GGA) [33]. The core states have been recalculated after each iteration. The calculations are partially scalar-relativistic in the sense that although the wave functions are non-relativistic, first-order perturbation corrections to the energy eigenvalues due to the Darwin and the mass–velocity terms are included. The atomic sphere radii of Mg (Zn), C and Ni were kept as 1.404, 0.747, and 0.849 of the Wigner–Seitz radius, respectively. The vacancies in the C sub-lattice are modelled with the help of empty spheres, and their radius is kept the same as that of C itself. The overlap volume resulting from the blow up of the atomic spheres was less than 15%, which is legitimate within the accuracy of the approximation [34].

The electron–phonon coupling parameter  $\lambda$  can be expressed as  $\eta/M\langle\omega^2\rangle$ , where  $\eta$  is the Hopfield parameter, expressed as the product of  $N(E_F)$  and the mean square electron–ion matrix element  $\langle I^2 \rangle$ , with  $M$  and  $\langle\omega^2\rangle$  being the ionic mass and average phonon frequency [35]. However, one may note that the above decomposition of the problem into electronic and phonon contributions is only approximate since in principle  $\langle\omega^2\rangle$  is also determined by the electronic states. It follows that the Hopfield parameter is the most simple basic quantity which one may obtain from first principles as suggested by Gaspari and Gyorffy [36]. The latter assumes a rigid muffin-tin approximation (RMTA) in which the potential enclosed by a sphere rigidly moves with the ion and the change in the crystal potential, caused by the displacement, is given by the potential gradient. Within the RMTA the spherically averaged part of the Hopfield parameter may be calculated as

$$\eta_0 = \frac{2}{N(E_F)} \sum_l (l+1) M_{l,l+1}^2 \frac{N_l(E_F) N_{l+1}(E_F)}{(2l+1)(2l+3)} \quad (1)$$

where  $N(E_F)$  is the total density of state per spin at the Fermi energy, and  $N_l$  the  $l$ th partial density of state calculated at the Fermi energy  $E_F$ , on the site considered. The term  $M_{l,l+1}$  is the electron–phonon matrix element given as [27]

$$M_{l,l+1} = \int_0^S r^2 R_l \frac{dV}{dr} R_{l+1} dr \quad (2)$$

which is obtained from the gradient of the potential and the radial solutions  $R_l$  and  $R_{l+1}$  of the Schrodinger equation evaluated at  $E_F$ . The special form of equations (1) and (2) stems from the ASA in which the radial wave functions are normalized to unity in the atomic sphere of radius  $S$ , i.e.,  $\int_0^S r^2 R_l^2(r) dr = 1$ . In the ASA,  $M_{l,l+1}$  is expressed in terms of logarithmic derivatives  $D_l = r R_l' / R_l$  evaluated at the sphere boundary. Skriver and Mertig derive the expression for  $M_{l,l+1}$  as

$$M_{l,l+1} = -\phi_l(E_F) \phi_{l+1}(E_F) \{ [D_l - l] [D_{l+1} + l + 2] + [E_F - V(S)] S^2 \} \quad (3)$$

where  $V(S)$  is the one-electron potential and  $\phi_l(E_F)$  the sphere boundary amplitude of the  $l$  partial wave evaluated at  $E_F$ .

Numerical estimates of the magnetic energy were carried out using the fixed-spin-moment method [25]. In the fixed-spin-moment method the total energy is obtained for a given magnetization  $M$ , i.e., by fixing the numbers of electrons with up and down spins. In this case, the Fermi energies in the up and down spin bands are not equal to each other because

the equilibrium condition would not be satisfied for arbitrary  $M$ . At the equilibrium  $M$  two Fermi energies will coincide with each other. The total magnetic energy becomes minimum or maximum at this value of  $M$ . Note that the two approaches, i.e., the self-consistent, floating-spin-moment method and the fixed-spin-moment method, are equivalent in the sense that for a given lattice constant the magnetic moment calculated by the standard floating-spin-moment approach is the same as the magnetic moment for which the fixed-spin-moment total energy has its minimum [37]. In practice, the floating-spin-moment approach sometimes runs into some convergence problems. From experience, to avoid such predicaments in convergence, one may carefully monitor the mixing of the initial and final charges during the iterations and increase the number of  $\mathbf{k}$ -points. Thus, for a better resolution to determine the change in the total energy with respect to the input magnetization, the  $\mathbf{k}$ -mesh had 1771  $\mathbf{k}$ -points in the irreducible wedge of the cubic Brillouin zone.

By the fixed-spin-moment method the difference  $\Delta E(M)$  ( $=E(M) - E(0)$ ) for given values of  $M$  is calculated. The calculated  $\Delta E(M)$  is fitted to the phenomenological Landau equation of phase transition which is given as

$$\Delta E(M) = \sum_{n>0} \frac{1}{2n} a_{2n} M^{2n} \quad (4)$$

for  $n = 3$ , where the sign of the coefficient  $a_{2n}$  for  $n = 1$  determines the nature of the magnetic ground state, i.e.,  $a_2 > 0$  refers to a paramagnetic ground state while  $a_2 < 0$  refers to a ferromagnetic phase. We have applied the approach described above to the study of carbon vacancies in  $\text{MgCNi}_3$  [13] and 3d transition-metal– $\text{MgCNi}_3$  alloys [14].

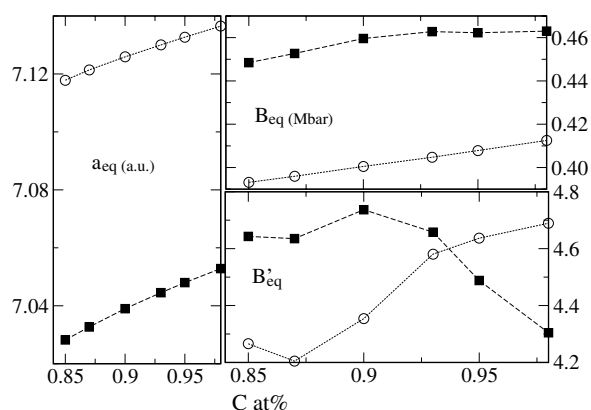
### 3. Results and discussion

#### 3.1. Equation of state

Both x-ray and neutron diffraction techniques unambiguously report  $\text{MgCNi}_3$  and  $\text{ZnCNi}_3$  as cubic perovskites with their lattice constants determined as 7.201 and 6.918 au, respectively. Assuming an underlying rigid cubic lattice, with Mg (Zn) at the cube corners, Ni at the faces and C at the octahedral interstitial site, total energy minimization was carried out to determine the equation of state parameters. The total energies calculated, self-consistently, for six lattice constants close to equilibrium were fed as input to a third-order Birch–Murnaghan equation of state [38, 39]. Note that the Birch–Murnaghan equation is derived from the theory of finite strain, by considering an elastic isotropic medium under isothermal compression, with the assumption that the pressure–volume relation remains linear. Hence, in the optimization procedure we have restricted the choice close to the equilibrium.

Since the choice of the exchange correlation potential in the Kohn–Sham Hamiltonian has proven to be sensitive in the structural characterization, we have carried out the total energy minimization for two different approximations, namely the LDA and GGA [32, 33]. The results are shown in table 1. The GGA considerably overestimates the lattice constant for both alloys, when compared to the experimental values. For  $\text{MgCNi}_3$ , using the LDA description of the exchange–correlation, the lattice constant was calculated as 7.139 au, with the bulk modulus and its pressure derivative as 0.42 Mbar and 4.78, respectively. These values are consistent with the earlier first-principles reports [4, 6]. The underestimation in the lattice constant for  $\text{MgCNi}_3$ , however, when compared to the experiments, is due to the over-binding effects in the LDA, and is a well known problem.

For  $\text{ZnCNi}_3$  the equilibrium lattice constant calculated using LDA yielded the value as 7.056 au, which, when compared to the recent x-ray diffraction results [2] of 6.918 au, was



**Figure 1.** The variation in the equation of state parameters, equilibrium lattice constant  $a_{\text{eq}}$  (au), the bulk modulus  $B_{\text{eq}}$  (Mbar) and the pressure derivative of the bulk modulus, as a function of  $y$  in  $\text{MgC}_y\text{Ni}_3$  (open circles) and  $\text{ZnC}_y\text{Ni}_3$  (filled squares) calculated using the KKR-ASA-CPA method as described in the text.

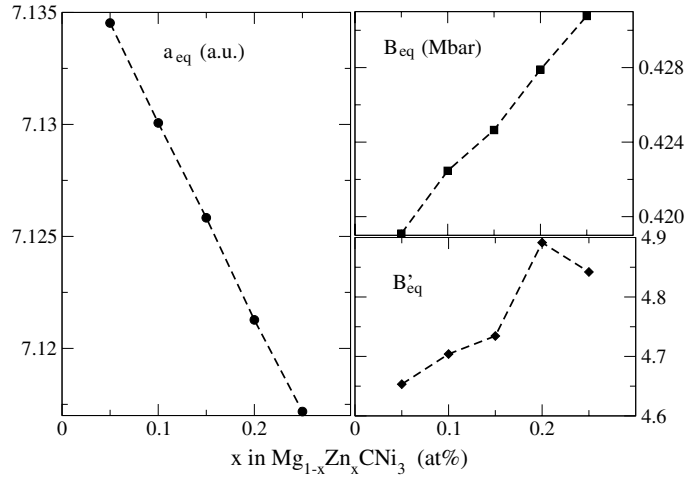
**Table 1.** Comparison of the equation of state parameters of cubic perovskite  $\text{ZnCNi}_3$  with that of  $\text{MgCNi}$  using the KKR-ASA method as described in the text.

	GGA		LDA	
	$\text{ZnCNi}_3$	$\text{MgCNi}_3$	$\text{ZnCNi}_3$	$\text{MgCNi}_3$
$a_{\text{eq}}$ (au)	7.2255	7.3041	7.0558	7.1387
$B_{\text{eq}}$ (Mbar)	0.3886	0.3479	0.4656	0.4188
$B'_{\text{eq}}$	4.4106	4.5255	4.3444	4.7813

found to be an overestimation. However, the results of the present calculations are consistent with the works of Johannes and Pickett [3] who employed the FP-LAPW method. Note that the consistency of the ASA calculations with that of the full-potential counterparts are due to the inclusion of the muffin-tin correction [28]. The KKR-ASA calculations further finds the bulk modulus and its pressure derivative of  $\text{ZnCNi}_3$  as 0.46 Mbar and 4.34, respectively. As mentioned above, the overestimation of the lattice constant in the LDA is not so common, which suggests that the samples subjected to the experiments may be sub-stoichiometric. This was also emphasized by Johannes and Pickett [3] following the crystal structure characterization of  $\text{MgC}_y\text{Ni}_3$  alloys [8]. In the latter, both experiments [8, 12] and theoretical calculations [13] have shown that the lattice constant decreases as the C content in the material decreases.

To look for the changes in the equation of state parameters as a function of C content in  $\text{MgC}_y\text{Ni}_3$  and  $\text{ZnC}_y\text{Ni}_3$  alloys, total energy minimization was carried out. The variation is shown in figure 1. For both  $\text{MgC}_y\text{Ni}_3$  and  $\text{ZnC}_y\text{Ni}_3$  alloys, the lattice constant as well as the bulk modulus decrease as the C atomic percentage decreases. For  $\text{MgC}_y\text{Ni}_3$ , the observed trend is consistent with the earlier x-ray diffraction measurements. The rate of decrease in the lattice constant is estimated as 0.142 au/at.% C while for  $\text{ZnC}_y\text{Ni}_3$ , the lattice constant was found to decrease at the rate of 0.189 au/at.% C. Though the lattice constant and bulk modulus showed similar trends for both alloys, the change in the pressure derivative of the bulk modulus as a function of  $y$  characteristically differed.

The pressure derivative of the bulk modulus measures the rate at which the material becomes incompressible with increasing pressure, and is sensitive to the softness of the



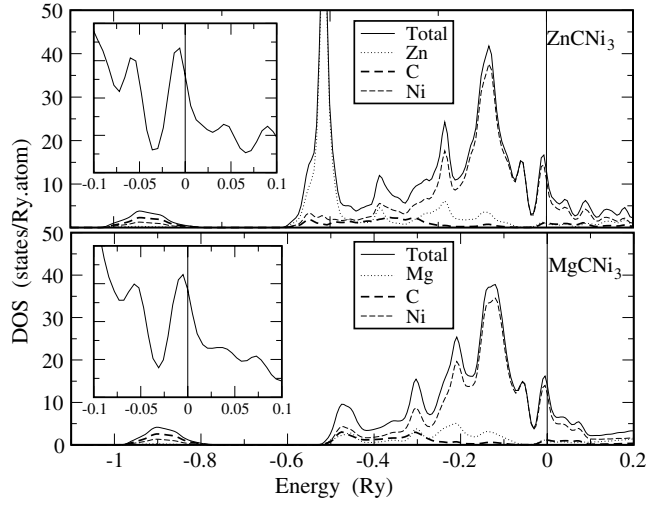
**Figure 2.** The variation in the equation of state parameters, equilibrium lattice constant  $a_{\text{eq}}$  (au), the bulk modulus  $B_{\text{eq}}$  (Mbar) and the pressure derivative of the bulk modulus, as a function of  $x$  in  $\text{Mg}_{1-x}\text{Zn}_x\text{CNi}_3$  calculated using the KKR-ASA-CPA method as described in the text.

equation of state. In the Debye approximation for isotropic solids, which assumes a uniform dependence of the lattice frequencies with volume, one may express the average phonon frequency  $\omega$  as  $B'_{\text{eq}} \propto \frac{\delta \ln \omega}{\delta \ln V}$ , where  $V$  is the equilibrium volume of the unit cell. Note that volume for the vacancy-rich alloys decreases with decreasing  $y$ , while  $B'_{\text{eq}}$  maps a different trend for  $\text{MgC}_y\text{Ni}_3$  and  $\text{ZnC}_y\text{Ni}_3$  alloys. Such a behaviour indicates that the properties associated with the  $\text{MgC}_y\text{Ni}_3$  lattice could be characteristically different from that of the  $\text{ZnC}_y\text{Ni}_3$  counterparts. Also, one may note that the phonon spectrum for  $\text{MgCNi}_3$  reveals that certain C modes play a vital role in the materials superconducting properties in addition to those of the Ni modes [40, 41].

Partial replacement of Zn for Mg in  $\text{MgCNi}_3$  has shown that the transition temperature decreases [42]. The findings also conclude that the nature of the pairing mechanism in  $\text{MgCNi}_3$  is conventional [42]. To study the changes brought about by Zn substitutions in the Mg sublattice of  $\text{MgCNi}_3$ , we have carried out KKR-ASA-CPA calculations for  $\text{Mg}_{1-x}\text{Zn}_x\text{Ni}_3$  alloys. In figure 2, we show the variation of the equation of state parameters of  $\text{Mg}_{1-x}\text{Zn}_x\text{Ni}_3$  alloys. The decrease in the lattice constant is consistent with the previous experimental report. The bulk modulus as well as its pressure derivative increases as  $x$  increases in  $\text{Mg}_{1-x}\text{Zn}_x\text{Ni}_3$  alloys. This clearly indicates that the average phonon frequency gets modulated as Zn replaces Mg in  $\text{MgCNi}_3$ .

### 3.2. Electronic structure

In figure 3, we show the total and sub-lattice resolved partial densities of states of  $\text{MgCNi}_3$  and  $\text{ZnCNi}_3$  calculated at their respective equilibrium lattice constants. The characteristic features of both  $\text{MgCNi}_3$  and  $\text{ZnCNi}_3$  appear more or less similar with the exception of a sharp peak in the energy range  $-0.6 \leq E \leq -0.4$ , characteristic of Zn 3d states. Being very low on the energy scale compared to the Fermi energy, which is zero on the scale shown, one may expect Zn d states to be localized and thus behave atomically, while for  $\text{MgCNi}_3$  a small peak characteristic of the Mg–Ni bonding also appears in this energy range, but is less pronounced. Furthermore, the states near  $E_F$  are predominantly Ni 3d in character in both alloys, with little



**Figure 3.** Comparison of the total and sub-lattice resolved partial densities of states of  $\text{ZnCNi}_3$  and  $\text{MgCNi}_3$ , calculated at their respective equilibrium lattice constants. The vertical line through energy zero represents the alloy Fermi energy. In the inset we show an enlargement of the total density of states near the Fermi energy.

**Table 2.** Comparison of the total  $N(E_F)$  and sub-lattice resolved densities of states of  $\text{ZnCNi}_3$  and  $\text{MgCNi}_3$  expressed in units of states/Ryd atom.

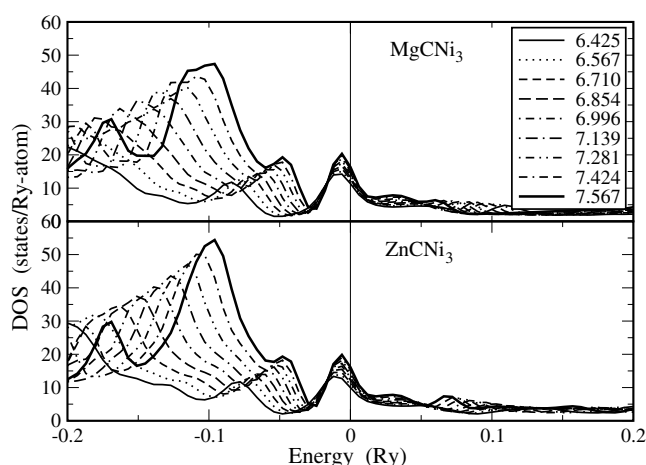
	$N(E_F)$	Zn(Mg)	C	Ni	Ni $d_{xy(xz)}$	Ni $d_{yz}$	Ni $d_{x^2-y^2}$	Ni $d_{3z^2-1}$
$\text{ZnCNi}_3$	13.005	0.945	1.076	10.984	4.002	0.168	1.296	0.606
$\text{MgCNi}_3$	14.557	1.016	1.199	12.341	4.509	0.097	1.474	0.658

admixture of the C 2p states. One may also find that the position of the Ni 3d derived singularity is slightly lower in the energy scale for  $\text{ZnCNi}_3$  than for  $\text{MgCNi}_3$ , which is consistent with the previous results. The  $N(E_F)$  and the contributions to it from the sub-lattices are compared in table 2.

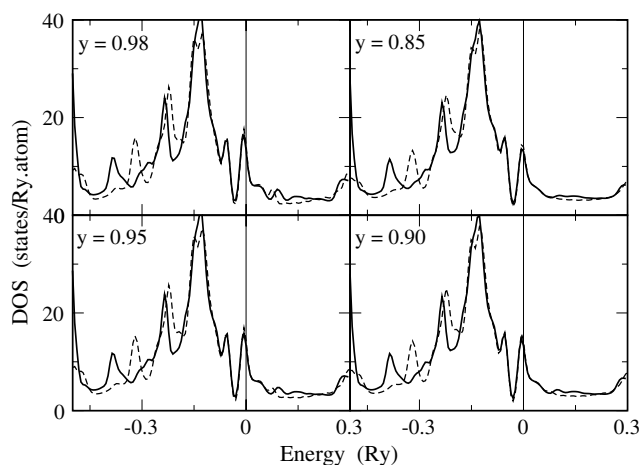
The reported values of  $N(E_F)$  for  $\text{MgCNi}_3$  are at variance with the existing reports [4–7, 43–47]. It appears that the value is sensitive to the basic approximations made in each type of the electronic structure method, and also to the parameters like that of the choice of Wigner–Seitz radii, choice of the exchange–correlation potential, and others. However, under similar approximations, it is clear that for  $\text{ZnCNi}_3$  the  $N(E_F)$  reduces by 12% in comparison with  $\text{MgCNi}_3$ . This is consistent with the earlier first-principles FP-LAPW calculations [3]. The reduction in  $N(E_F)$  may be largely due to the smaller lattice constant of  $\text{ZnCNi}_3$ , in comparison with  $\text{MgCNi}_3$ . The change in the density of states, as well as in the  $N(E_F)$ , as a function of lattice constant is shown in figure 4. Approximating the variation of  $N(E_F)$  to be linear with respect to the lattice constant, we find  $dN(E_F)/da$  to be 20.46 and 22.02 states/Ryd atom/au for  $\text{MgCNi}_3$  and  $\text{ZnCNi}_3$ , respectively.

To understand the changes in the electronic structure upon the introduction of C vacancies, in figures 5–8 we show the changes in the total and sub-lattice resolved C 2p and Ni 3d partial densities of states of  $\text{ZnC}_y\text{Ni}_3$  and  $\text{MgC}_y\text{Ni}_3$  alloys calculated at their equilibrium lattice constants. It follows from the figures that the change in the distribution of states is more or less insignificant near the Fermi energy, but states lower in energy undergo substantial changes.



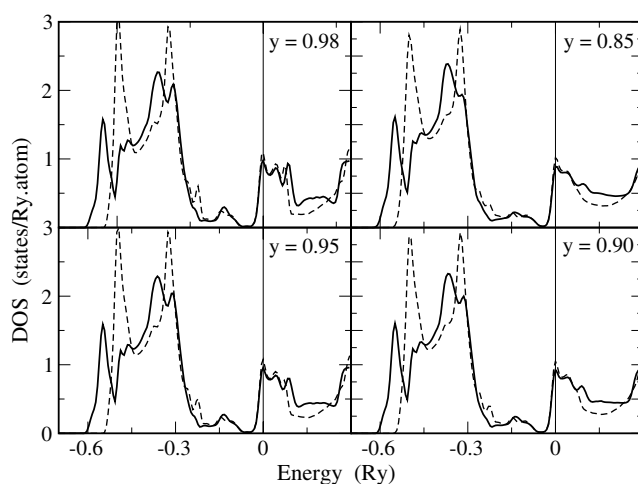


**Figure 4.** Comparison of the change in the total density of states near the Fermi energy of  $\text{ZnCNi}_3$  and  $\text{MgCNi}_3$  for a range of lattice constants as indicated in the figure. The vertical line through energy zero represents the alloy Fermi energy.

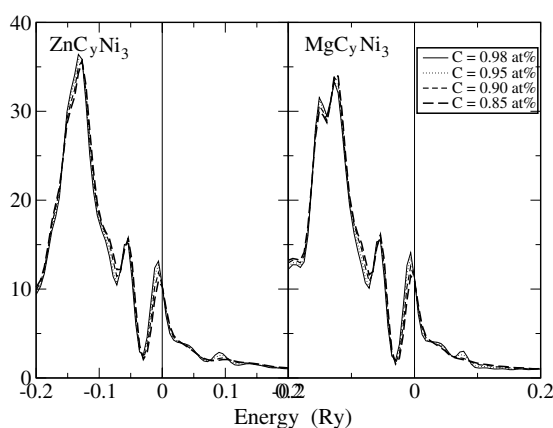


**Figure 5.** Comparison of the change in the total density of states of  $\text{ZnC}_y\text{Ni}_3$  (solid line) and  $\text{MgC}_y\text{Ni}_3$  (dashed lines) alloys calculated at their equilibrium lattice constant with  $y$  as indicated. The vertical line through energy zero in each panel represents the Fermi energy.

Upon the creation of vacancies, a few of the C 2p–Ni 3d bonds break, and result in charge redistribution. Note that the  $\text{CNi}_6$  octahedron is a covalently built complex to which the cations at the cube corners (Zn and Mg) are thought to have donated their outermost valence electrons. The crystal geometry suggests six Ni atoms as the first nearest neighbours to C and eight Mg/Zn atoms as second nearest neighbours. For Ni the second nearest coordination shell carries four Mg/Zn atoms. The charge redistribution arising due to the breaking of the p–d bonds would be proportional to the electro-positivity of the cation-Mg/Zn. Since Mg is more electropositive than Zn, charge redistribution to the Mg/Zn sub-lattices, as a function of vacancies, would be more significant in  $\text{MgCNi}_3$  when compared to  $\text{ZnCNi}_3$ . This is consistent with the fact that a larger fraction of the charge would be transferred back to the Mg sub-lattice in  $\text{MgCNi}_3$  in comparison with that of the Ni sub-lattice.



**Figure 6.** Comparison of the change in the sub-lattice resolved C 2p partial density of states of  $\text{ZnC}_y\text{Ni}_3$  (solid line) and  $\text{MgC}_y\text{Ni}_3$  (dashed lines) alloys calculated at their equilibrium lattice constant with  $y$  as indicated. The vertical line through energy zero in each panel represents the Fermi energy.

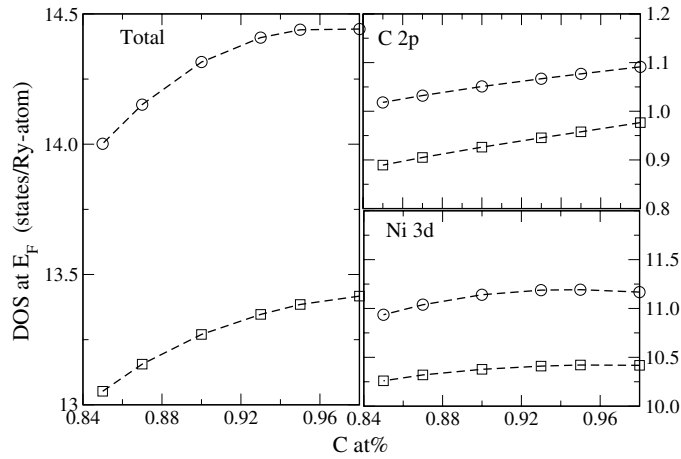


**Figure 7.** Comparison of the change in the sub-lattice resolved Ni 3d partial density of states of  $\text{ZnC}_y\text{Ni}_3$  and  $\text{MgC}_y\text{Ni}_3$  alloys, over a small energy window around the Fermi energy, calculated at their equilibrium lattice constant with  $y$  as indicated. The vertical line through energy zero in each panel represents the Fermi energy.

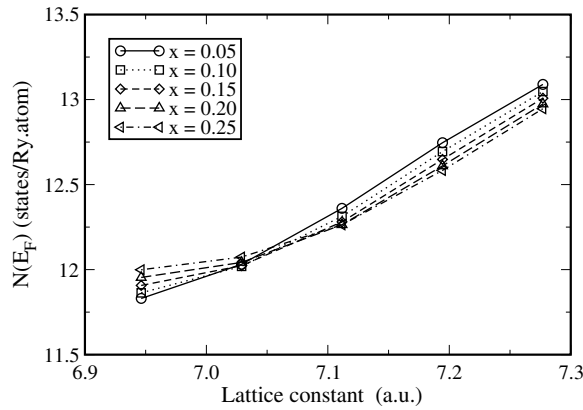
The change in the  $N(E_F)$  as a function of lattice constant in  $\text{Mg}_{1-x}\text{Zn}_x\text{CNi}_3$  alloys is shown in figure 9. One may find that  $N(E_F)$  decreases for all values of  $x$ , with respect to lattice constant. However,  $N(E_F)$  as a function of  $x$ , at the equilibrium lattice constant, was found to deviate a little, as is evident from figure 9. This clearly suggests that the electronic structure properties are mainly governed by the  $\text{CNi}_6$  octahedra. The atoms occupying the cube corners, i.e., Mg and Zn, however, play a non-trivial role in determining the structural properties.

### 3.3. Hopfield parameter

The Hopfield parameter  $\eta$  has been regarded as a local ‘chemical’ property of an atom in a crystal. It has been emphasized earlier that the most significant single parameter in



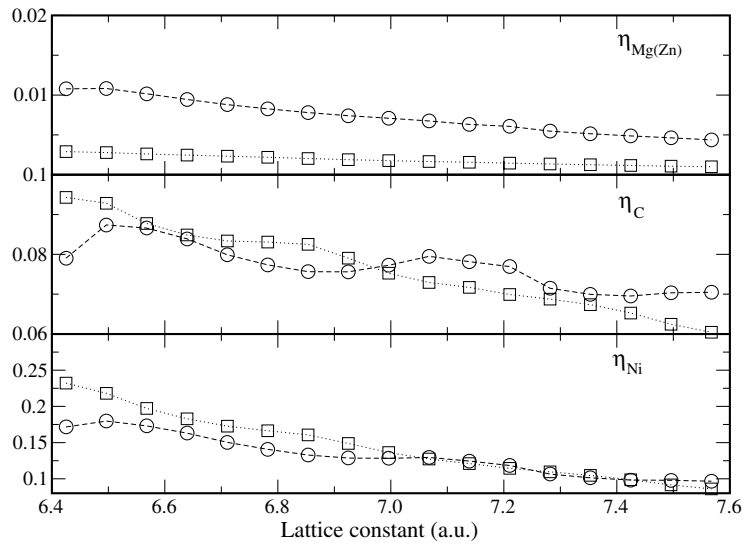
**Figure 8.** Comparison of the change in the total, sub-lattice resolved C 2p and Ni 3d partial densities of states at  $E_F$  of  $ZnC_yNi_3$  (squares) and  $MgC_yNi_3$  (circles) as a function of  $y$ .



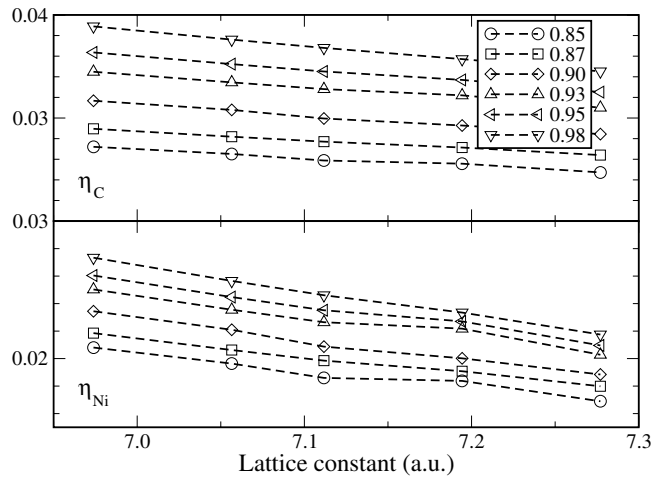
**Figure 9.** The change in the total density of states at the Fermi energy,  $N(E_F)$ , in units of states/Ryd atom as a function of lattice constant in  $Mg_{1-x}Zn_xCNi_3$  alloys. The values of  $x$  are as shown in the figure.

understanding the  $T_C$  of a conventional superconductor is the Hopfield parameter [35]. For strong-coupling systems, the variation in  $\eta$  is more important than the variation of  $\langle\omega^2\rangle$  in changing  $T_C$ . Softening  $\langle\omega^2\rangle$  often does enhance  $T_C$ , but a significant change in the magnitude of  $T_C$  depends largely on a significant change in the  $\eta$  value rather than a small change in the corresponding  $\langle\omega^2\rangle$ . As a matter of fact, we look for the changes in  $\eta$  from the three sub-lattices of these perovskites as a function of lattice constant as well as  $y$  in  $MgC_yNi_3$  and  $ZnC_yNi_3$  alloys. Note that for  $MgCNi_3$ , it has been reported that the superconducting transition temperature  $T_C$  increases upon application of external pressure [48, 49]. Besides, experiments remain controversial on the strength of the electron–phonon interaction in  $MgCNi_3$  [50, 51, 48, 52]. It has been suggested that  $MgCNi_3$  may be a strongly coupled superconductor, however, with the magnitude of  $T_C$  being marginally reduced due to the paramagnon interactions [4, 51].

In figure 10 we show the changes in  $\eta$  of  $MgCNi_3$  and  $ZnCNi_3$  as a function of lattice constant. It is clear from figure 10 that  $\eta_C$  and  $\eta_{Ni}$  linearly increase as a function of decreasing



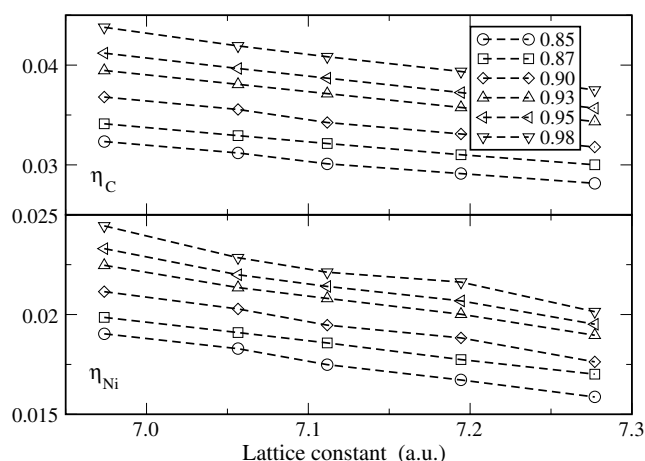
**Figure 10.** Comparison of the change in  $\eta_{\text{Mg/Zn}}$ ,  $\eta_{\text{C}}$  and  $\eta_{\text{Ni}}$  as a function of lattice constant of  $\text{MgCNi}_3$  (circles) and  $\text{ZnCNi}_3$  (squares).



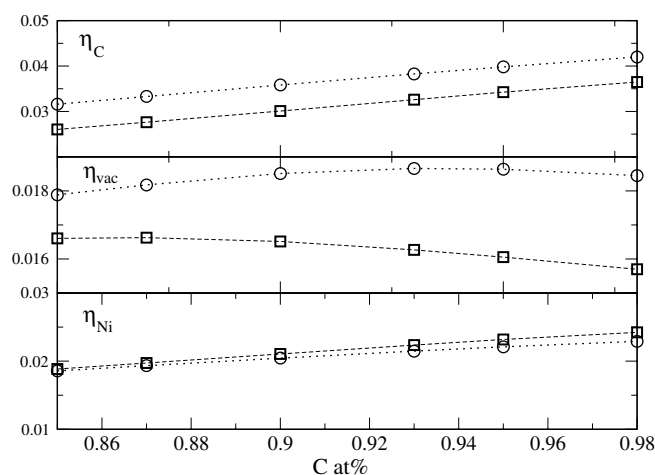
**Figure 11.** The change in  $\eta_{\text{C}}$  (upper panel) and  $\eta_{\text{Ni}}$  (lower panel) as a function of lattice constant in  $\text{MgC}_y\text{Ni}_3$  alloys with  $y$  as indicated.

volume in either alloys. If the change in the average phonon frequency remains small, then either of these alloys could enhance the transition temperature with respect to external pressure. For  $\text{MgCNi}_3$  this view is consistent with the previous experimental results. A similar characteristic feature holds for the vacancy-rich disordered alloys, the variation of which is shown in figures 11 and 12.

To have an understanding in the variation of  $\eta_{\text{C}}$ ,  $\eta_{\text{vac}}$  and  $\eta_{\text{Ni}}$ , where  $\eta_{\text{vac}}$  can be considered as the local chemical property of the electrons in the empty sphere, we show in figure 13 the change in these parameters as a function of  $y$  in both  $\text{MgC}_y\text{Ni}_3$  and  $\text{ZnC}_y\text{Ni}_3$  alloys. One may find that the variation of  $\eta$  remains similar for both the alloys as a function of decreasing C content.



**Figure 12.** The change in  $\eta_C$  (upper panel) and  $\eta_{Ni}$  (lower panel) as a function of lattice constant in  $ZnC_yNi_3$  alloys with  $y$  as indicated.

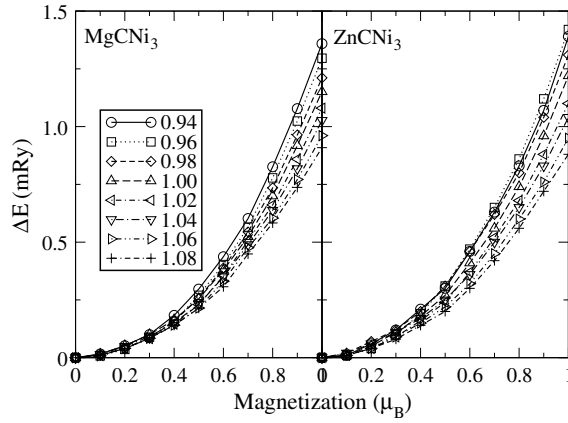


**Figure 13.** Comparison of the change in  $\eta_C$ ,  $\eta_{vac}$  and  $\eta_{Ni}$  as a function of  $y$  in  $ZnC_yNi_3$  (squares) and  $MgC_yNi_3$  (circles) alloys.

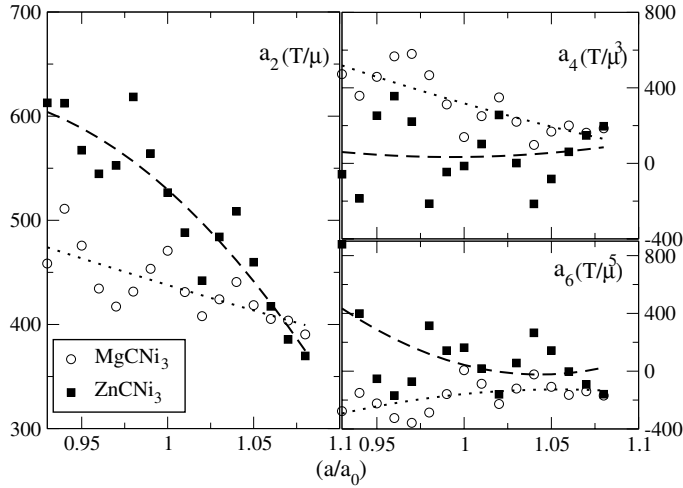
### 3.4. Magnetic properties

Total energies from both the self-consistent, spin-polarized and spin-unpolarized calculations remain degenerate for  $MgCNi_3$  and  $ZnCNi_3$  alloys at their equilibrium lattice constants. This unambiguously shows that the materials are non-magnetic in nature. However, having suggested that  $MgCNi_3$  is on the verge of a ferromagnetic instability [4, 5, 51, 53, 54], and also that incipient magnetism in the form of spin-fluctuations resides in the material, we attempt to compare the magnetic properties of  $MgCNi_3$  and  $ZnCNi_3$  alloys using the fixed-spin-moment approach of alloy theory [25].

Numerical calculations of magnetic energy  $\Delta E(M)$  for  $MgCNi_3$  and  $ZnCNi_3$  were carried out at over a range of lattice constants. The calculated results of  $\Delta E(M)$  in the fixed-spin-moment method are shown in figure 14. The calculated  $\Delta E(M)$  curves are fitted to the form of a power series of  $M^{2n}$  up to  $n = 3$ , for the polynomial as mentioned above. The variations



**Figure 14.** Comparison of the change in the magnetic energy as a function of magnetization in  $\text{MgCNi}_3$  and  $\text{ZnCNi}_3$  alloys for a range of lattice constant ratio  $a/a_{\text{eq}}$ , where  $a_{\text{eq}}$  is the equilibrium lattice constant of the respective alloys.



**Figure 15.** Comparison of the changes in the Landau coefficients  $a_2$ ,  $a_4$  and  $a_6$  as a function lattice constant in  $\text{MgCNi}_3$  and  $\text{ZnCNi}_3$  alloys. The open circles and filled squares are the calculated values and the best quadratic fits representing these points are shown with dotted and dashed lines, respectively, for  $\text{MgCNi}_3$  and  $\text{ZnCNi}_3$  alloys.

of the coefficients,  $a_2$  in units of  $\frac{T}{\mu_B}$ ,  $a_4$  in  $\frac{T}{\mu_B^3}$ , and  $a_6$  in  $\frac{T}{\mu_B^5}$  as a function of lattice constant, are shown in figure 15. The propensity of magnetism can be inferred from the sign of the coefficient which is quadratic in  $M$ , i.e.,  $a_2$ . The coefficient  $a_2$  is the measure of the curvature and it is positive definite when the total energy minimum is at  $M = 0$ , thus referring to a paramagnetic ground state. In general, when  $a_2$  becomes negative, it infers that there would exist a minimum in the  $\Delta E-M$  curve at a value other than  $M = 0$ , referring to a ferromagnetic phase at that value of  $M$ . The higher-order coefficients  $a_4$  and  $a_6$  however are significant and they control the variation of  $\Delta E$  with respect to  $M$ . For example, for larger values of  $M$ ,  $a_4$  and successively  $a_6$  would dominate, and if  $a_4(a_6)$  tends to be negative it would show a dip in the  $\Delta E-M$  variation pointing towards a magnetic transition at a higher value of  $M$ . This, in

the first-principles characterization of the magnetic properties of a material, would refer to a possibility of a metastable phase at relatively large values of external magnetic fields. However, it has to be noted that calculations for large values of  $M$  can result in ambiguous results. Hence, it is suggested to carry out calculations for smaller values of  $M$  and use the above-mentioned polynomial function up to the minimum order, where the curve fits with sufficient accuracy.

Figure 15 shows that for smaller values of lattice constant, the alloys show an enhanced paramagnetic character. One may also note that the variations in  $a_4$  and  $a_6$  coefficients are oppositely complemented, and hence in the renormalized approach to include corrections due to spin-fluctuations, as suggested by Yamada and Terao [55], they would cancel out in proportion, preserving the trend in the variation of  $a_2$ . Thus, it becomes likely that the incipient magnetic properties associated with  $\text{MgCNi}_3$  and  $\text{ZnCNi}_3$  would decrease as a function of decreasing lattice constant.

#### 4. Conclusions

First-principles studies of the electronic properties of  $\text{MgCNi}_3$  and  $\text{ZnCNi}_3$ , and also their non-stoichiometric alloys, have been carried out using the density-functional-based KKR-ASA method. We find that the lattice constant for  $\text{ZnCNi}_3$  is overestimated, while for  $\text{MgCNi}_3$  it is underestimated. This suggests that the material  $\text{ZnCNi}_3$  subjected to experiments may be non-stoichiometric. As a function of decreasing C content in  $\text{MgC}_y\text{Ni}_3$  and  $\text{ZnC}_y\text{Ni}_3$  alloys, one finds an opposite trend in the variation of pressure derivative of the bulk modulus, which is proportional to the averaged phonon frequency. With the electronic structure remaining essentially the same for  $\text{MgC}_y\text{Ni}_3$  and  $\text{ZnC}_y\text{Ni}_3$ , the results hint that non-stoichiometry may have opposite effects. Note that for  $0.9 < y < 1.0$ ,  $\text{MgC}_y\text{Ni}_3$  alloys are feebly superconducting, while according to the conjecture that has been made  $\text{ZnC}_y\text{Ni}_3$  is not. It can thus be inferred that the associated phonon modes in  $\text{ZnCNi}_3$  and its disordered alloys may be characteristically different when compared to the  $\text{MgCNi}_3$  counterparts. A comparison of the phonon spectra of these alloys thus become quite necessary to understand the absence of superconductivity in  $\text{ZnCNi}_3$ , although it is iso-structural and iso-valent with  $\text{MgCNi}_3$ .

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